

**FIXED POINT THEOREMS FOR MULTIVALUED
MAPPINGS RELATED TO SOME GEOMETRIC
PROPERTIES IN SOME METRIC SPACES**

BANCHA PANYANAK

**A THESIS SUBMITTED TO THE GRADUATE SCHOOL IN
PARTIAL FULFILLMENT OF THE REQUIREMENTS
FOR THE DEGREE OF
DOCTOR OF PHILOSOPHY
IN MATHEMATICS**

ลิขสิทธิ์มหาวิทยาลัยเชียงใหม่

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**THIS THESIS HAS BEEN APPROVED
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