

**APPROXIMATION METHODS FOR COMMON FIXED  
POINTS OF A COUNTABLE FAMILY OF SOME  
GENERALIZED NONEXPANSIVE MAPPINGS  
AND EQUILIBRIUM PROBLEMS**

**PRASIT CHOLAMJIAK**

**DOCTOR OF PHILOSOPHY  
IN MATHEMATICS**

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**THE GRADUATE SCHOOL  
CHIANG MAI UNIVERSITY  
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**PRASIT CHOLAMJIAK**

**A THESIS SUBMITTED TO THE GRADUATE SCHOOL IN  
PARTIAL FULFILLMENT OF THE REQUIREMENTS  
FOR THE DEGREE OF  
DOCTOR OF PHILOSOPHY  
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