

**STRONG CONVERGENCE OF MODIFIED HALPERN  
ITERATIONS IN  $CAT(0)$  SPACES**

**ASAWATHEP CUNTAVEPANIT**

**DOCTOR OF PHILOSOPHY  
IN MATHEMATICS**

ลิขสิทธิ์มหาวิทยาลัยเชียงใหม่

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**THE GRADUATE SCHOOL  
CHIANG MAI UNIVERSITY**

**APRIL 2013**

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**A THESIS SUBMITTED TO THE GRADUATE SCHOOL IN  
PARTIAL FULFILLMENT OF THE REQUIREMENTS  
FOR THE DEGREE OF  
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THIS THESIS HAS BEEN APPROVED  
TO BE A PARTIAL FULFILLMENT OF THE REQUIREMENTS  
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Prof. Dr. Suthep Suantai

29 APRIL 2013

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## ACKNOWLEDGEMENTS

Contribution and support from many people helped me completion of this thesis, I would like to take this opportunity to express my appreciation to them.

First, I would like to express my deepest thank to my supervisor, Asst. Prof. Dr. Bancha Panyanak, for his initial idea, guidance and encouragement which enable me to carry out my study successfully.

This work contains a number of improvement based on comments and suggestions provided by Asst. Prof. Dr. Bancha Panyanak, Prof. Dr. Sompong Dhompongsa and Prof. Dr. Suthep Suantai. It is my pleasure to express my sincere thanks to them for their generous assistance.

I would like to express my deep gratitude to my beloved family for their love and encouragement throughout my graduate study.

Moreover, I would like to thank all of my teachers for my knowledges, skills and their previous valuable instructions while studying.

Finally, I greatly appreciate the Centre of Excellence in Mathematics the Commission on Higher Education, Thailand for financial support.

Asawathep Cuntavepanit