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LIST OF ABBREVIATIONS

CCD	Charge-coupled device
CMOS	Complementary metal-oxide-semiconductor
CONF	Confidence interval
FOV	Field of view
НТ	Hough transforms
IP camera	Internet protocol camera
IR-LED	Infrared light emitting diode
MAE	Mean absolute error
PCA	Principal component analysis
P-CR	Pupil-corneal reflection
RMSE	Root-mean-square error
RGB	Red, Green, Blue
SD	Standard deviation
2-D	Two-dimensional
3-D	Three-dimensional

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STATEMENT OF ORIGINALITY

- 1. A novel method requiring only a single camera for a three-dimensional eye gaze tracking using eye model is proposed. By computing the gray-level intensity of image patches, the eigenvalues of iris and the iris area, eye gaze distance can be estimated.
- 2. A new three-dimensional eye model is proposed for eye gaze tracking by using the proposed eye gaze distance estimation without camera calibration and user calibration.
- 3. The proposed method can improve the accuracy of eye gaze tracking system even under the condition when a user's head is not stationary.



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ข้อความแห่งการริเริ่ม

- วิทยานิพนธ์นี้ได้เสนอวิธีการใหม่ในการตรวจติดตามการเพ่งมองโดยใช้แบบจำลองตา 3 มิติ ด้วยกล้องเดี่ยว การประมาณระยะห่างทำได้โดยการกำนวณก่ากวามเข้มของแสงระดับเทาของ แผ่นภาพ โดยใช้ก่าลักษณะเฉพาะของม่านตาและการใช้พื้นที่ของม่านตา
- วิทยานิพนธ์นี้ได้เสนอแบบจำลองตา 3 มิติแบบใหม่ สำหรับการใช้งานการตรวจติดตามการ เพ่งมอง โดยใช้วิธีการประมาณระยะห่างของตาที่ได้เสนอ โดยไม่มีการปรับเทียบระบบและ การปรับเทียบผู้ใช้งาน
- วิธีการที่เสนอสามารถปรับปรุงค่าความถูกต้องของระบบการตรวจติดตามการเพ่งมองได้ดี มากขึ้นกว่าเดิม โดยศีรษะผู้ใช้งานสามารถเคลื่อนที่ได้

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