FACTORISABLE MONOID OF GENERALIZED HYPERSUBSTITUTIONS OF

TYPE $\tau = (n)$



GRADUATE SCHOOL CHIANG MAI UNIVERSITY JULY 2016

FACTORISABLE MONOID OF GENERALIZED HYPERSUBSTITUTIONS OF

TYPE $\tau = (n)$



A THESIS SUBMITTED TO CHIANG MAI UNIVERSITY IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY IN MATHEMATICS

GRADUATE SCHOOL, CHIANG MAI UNIVERSITY JULY 2016

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AMPIKA BOONMEE

THIS THESIS HAS BEEN APPROVED TO BE A PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY IN MATHEMATICS

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