FIXED POINT THEOREMS AND CONVERGENCE THEOREMS OF ISHIKAWA ITERATIONS FOR SOME GENERALIZED NONEXPANSIVE MAPPINGS IN $CAT(\kappa)$ SPACES

BANCHA NANJARAS

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GRADUATE SCHOOL CHIANG MAI UNIVERSITY APRIL 2016

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A THESIS SUBMITTED TO CHIANG MAI UNIVERSITY IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY IN MATHEMATICS

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THIS THESIS HAS BEEN APPROVED TO BE A PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY IN MATHEMATICS

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ii

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