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 $K, \max$ 



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#### LIST OF ABBREVIATIONS AND SYMBOLS

- Time-delay τ
- Depth-of-cut parameter  $b_{\kappa}$
- Maximum stable depth-of-cut parameter  $b_{K,\max}$
- Ω Tool rotational speed
- Zero vibration mean chip thickness  $h_m$
- Instantaneous mean chip thickness h(t)
- 2104279 Linear feed rate of the workpiece to the cutting tool f

 $f_t$ Feed per tooth

- Instantaneous cutting tool's rotational angle ø
- **Designed Control force** и
- Cutting force w
- Zero vibration cutting force  $W_0$
- System state vectors х
- Weighting function state vector  $X_r$
- Augmented system state vector ñ
- Closed-loop system state vector  $X_{cl}$
- Output measurement signals  $y_m$
- Displacement signals of a control actuator  $y_a$
- Displacement signals of a cutting actuator  $y_t$
- Strain signals Е
- Chatter frequency  $\omega_{c}$
- Flexible structure natural frequency  $\omega_n$
- λ Eigenvalues
- Т Transformation matrix
- Additive uncertainty  $\Delta_a$

- $\Delta_m$  Multiplicative uncertainty
- $W_r$  Weighting function
- $K_P$  Proportional feedback gain of PD controller
- $K_D$  Derivative feedback gain of PD controller
- *K* State feedback controller gain
- $K_0$  Current state feedback controller gain
- $K_{\tau}$  Delayed state feedback controller gain



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# ข้อความแห่งการริเริ่ม

- 1) การออกแบบตัวควบคุมที่เหมาะสมแบบใหม่สำหรับการควบคุมแบบแอ็กทิฟเพื่อควบคุม เสถียรภาพของการสั่นที่เกิดจากกระบวบการขึ้นรูปชิ้นงานภายใต้แบบจำลองของระบบหน่วง เวลา แง่มุมใหม่ที่ได้คือการสร้างเกณฑ์เสถียรภาพแบบโรบัสภายใต้ฟังก์ชันนัลของเลอปูนอฟ-คราซอฟสกี ซึ่งนำไปสู่เงื่อนไขของอสมการเมทริกซ์เชิงเส้น ที่สามารถสังเคราะห์ตัวควบคุม แบบสัญญาณป้อนกลับ วิธีการออกตัวควบคุมยังมีการใช้เงื่อนไขความโรบัสของความ คลาดเคลื่อนของแบบจำลองในช่วงของโครงสร้างพลศาสตร์ที่ย่านความถี่สูง ซึ่งถูกพิจารณาให้ เป็นความไม่แน่นอนเชิงโดเมนความถี่โดยผ่านพลศาสตร์ส่วนเพิ่มเติม ถึงแม้ว่าเทคนิคเหล่านี้ จะเคยมีการประยุกต์ใช้โดยแยกกันในงานวิจัยที่มีมาก่อนหน้านี้ แต่การใช้งานที่มีการรวม เทคนิคดังกล่าวเพื่อมาประยุกต์ใช้กับพลศาสตร์ของกระบวนการขึ้นรูปจริงยังคงเป็นสิ่งใหม่ที่ ยังไม่มีการศึกษามาก่อน
- แท่นทคสอบการกัดขึ้นรูปแบบใหม่ได้ถูกออกแบบสำหรับใช้ทคสอบตัวควบคุมแบบแอ็กทิฟ แท่นทคสอบถูกออกแบบภายใต้แบบจำลองพื้นฐานของโครงสร้างยืดหยุ่นของสปินเดิลและ คอกกัดชิ้นงาน และสามารถวัดข้อมูลได้อย่างครบถ้วนโดยผ่านเซนเซอร์ที่ถูกติดตั้งบนแท่น ตัวกระตุ้นแม่เหล็กไฟฟ้าถูกใช้เพื่อจำลองผลของการกัดชิ้นงานตามสมการพลศาสตร์ของการ กัดชิ้นงานที่ถูกกำหนด โดยการใช้ฮาร์ดแวร์กวบคุมเวลาทันที (real-time control hardware)

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#### STATEMENT OF ORIGINALITY

- 1) New optimized controller designs for active control of vibrational stability in machining processes based on linear time delay system models are proposed. The main novel aspect is the formulation of robust stability criterion based on Lyapunov Krasovskii functionals that lead to Linear Matrix Inequality conditions that can be used to synthesize feedback controllers. The controller design approach incorporates a robustness criterion where model error associated with high frequency structural dynamics is accounted for by a frequency domain uncertainty representation via augmented dynamics. Although similar techniques have been used separately in previous work by other researchers, their combined use and application to realistic machining dynamics is believed to be novel.
- 2) A new test facility has been designed and realized for the experiments on active control of machining vibration. This test system involves a simplified representation of a flexible milling spindle/tool structure that allows full monitoring via multiple sensor integration. An electromagnetic actuator can be used to emulate cutting effects according to any given cutting dynamics equations which are implemented by real-time control hardware.

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