

GLOBAL  
EDITION



# College Mathematics

*for Business, Economics, Life Sciences,  
and Social Sciences*

FOURTEENTH EDITION

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