



# ATOMS AND MOLECULES

## Interacting with Light

**Atomic Physics for the Laser Era**

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Peter van der Straten and Harold Metcalf

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# ATOMS AND MOLECULES INTERACTING WITH LIGHT

Atomic Physics for the Laser Era

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