




FORMULATION SIMPLIFIED

Finding the Sweet Spot through Design and
Analysis of Experiments with Mixtures

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