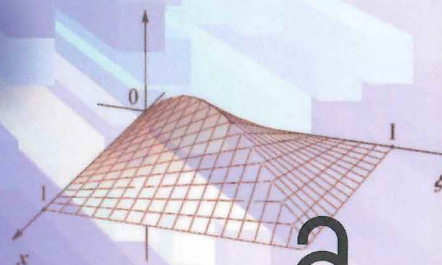
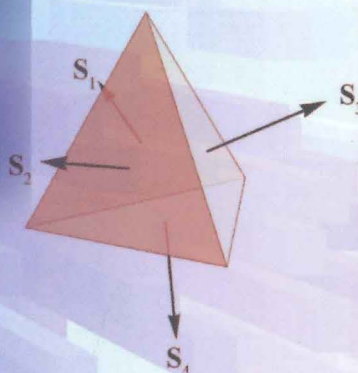
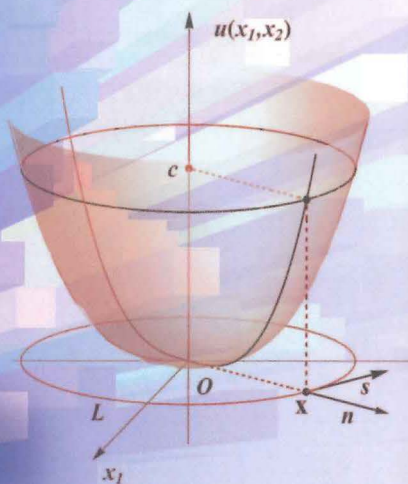
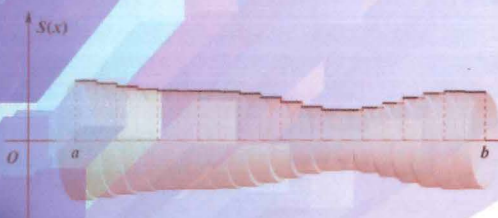


Vladimir Mityushev
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Natalia Rylko

Introduction to Mathematical Modeling and Computer Simulations



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