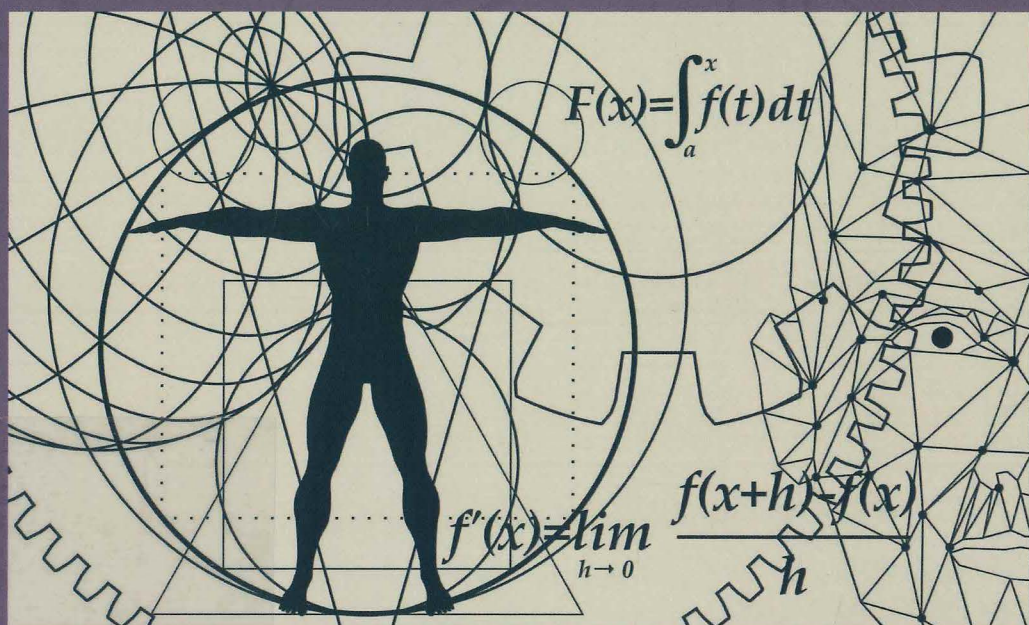


Advances in Applied Mathematics

ADVANCED MATHEMATICAL MODELING WITH TECHNOLOGY



William P. Fox
Robert E. Burks



CRC Press

Taylor & Francis Group

A CHAPMAN & HALL BOOK

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Advanced Mathematical Modeling with Technology



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 **CRC Press**
Taylor & Francis Group
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