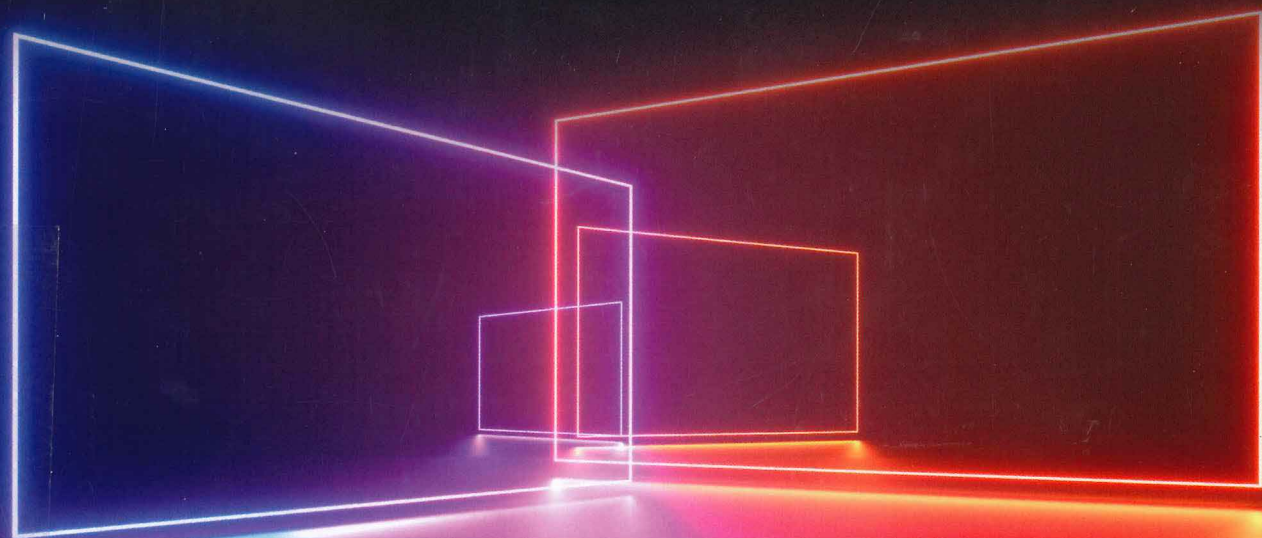


# PHYSICS, OPTICS, AND SPECTROSCOPY OF MATERIALS

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ZEEV BURSHTAIN



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# Physics, Optics, and Spectroscopy of Materials

Zeev Burshtein  
Ness Ziona, Israel



WILEY

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