TEXTBOOKS IN MATHEMATICS

Jeffery J. Leader

NUMERICAL ANALYSIS and SCIENTIFIC COMPUTATION

Second Edition

CRC Press
Taylor & Francis Group
A CHAPMAN & HALL BOOK

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CRC Press
Taylor & Francis Group
Boca Raton London New York

CRC Press is an imprint of the
Taylor & Francis Group, an **informa** business
A CHAPMAN & HALL BOOK

Contents

Preface ix

Preface to the 2nd Edition, Student xiii

Preface to the 1st Edition xv

Chapter 1. Nonlinear Equations 1
1. Bisection and Inverse Linear Interpolation 1
2. Newton's Method 11
3. The Fixed Point Theorem 21
4. Quadratic Convergence of Newton's Method 28
5. Modifications of Newton's Method 41
6. Brent's Method 51
7. Effects of Finite Precision Arithmetic 58
8. Polynomial Roots 70

Chapter 2. Linear Systems 81
1. Gaussian Elimination with Partial Pivoting 81
2. The LU Decomposition 93
3. The LU Decomposition with Pivoting 105
4. Newton's Method for Systems 120
5. The Cholesky Decomposition 131
6. Conditioning 143
7. The QR Decomposition and Least Squares 156
8. The QR Decomposition by Triangularization 168
9. The QR Decomposition by Orthogonalization 180
10. The Singular Value Decomposition 192

Chapter 3. Iterative Methods 199
1. Jacobi and Gauss-Seidel Iteration 199
2. Sparsity 211
3. Iterative Refinement 221
4. Preconditioning 227
5. Krylov Space Methods 233
6. Numerical Eigenproblems 246
7. The QR Method of Francis 254

Chapter 4. Polynomial Interpolation 265
1. Lagrange Interpolating Polynomials 265
2. Piecewise Linear Interpolation 280
3. Cubic Splines 292
4. Computation of the Cubic Spline Coefficients 302
5. Rational Function Interpolation 313
6. The Best Approximation Problem 322

Chapter 5. Numerical Integration 333
1. Closed Newton-Cotes Formulas 333
2. Open Newton-Cotes Formulas 348
3. Gaussian Quadrature 361
4. Gauss-Chebyshev Quadrature 373
5. Adaptivity and Automatic Integration 381
6. Automatic Integration with Gauss Rules 392
7. The Trapezoidal Rule with Extrapolation 401
8. Periodizing Transformations 410

Chapter 6. Differential Equations 421
1. Numerical Differentiation 421
2. Euler's Method 431
3. Improved Euler's Method 441
4. Analysis of Explicit One-Step Methods 448
5. Taylor and Runge-Kutta Methods 457
6. Adaptivity and Stiffness 466
7. Multi-step Methods 474

Chapter 7. Nonlinear Optimization 483
1. One-Dimensional Searches 483
2. The Method of Steepest Descent 491
3. Newton Methods for Nonlinear Optimization 500
4. Multiple Random Start Methods 509
5. Direct Search Methods 517
6. The Nelder-Mead Method 525
7. Conjugate Direction Methods 531
8. Hansen's Method 539

Afterword 549

Index 553