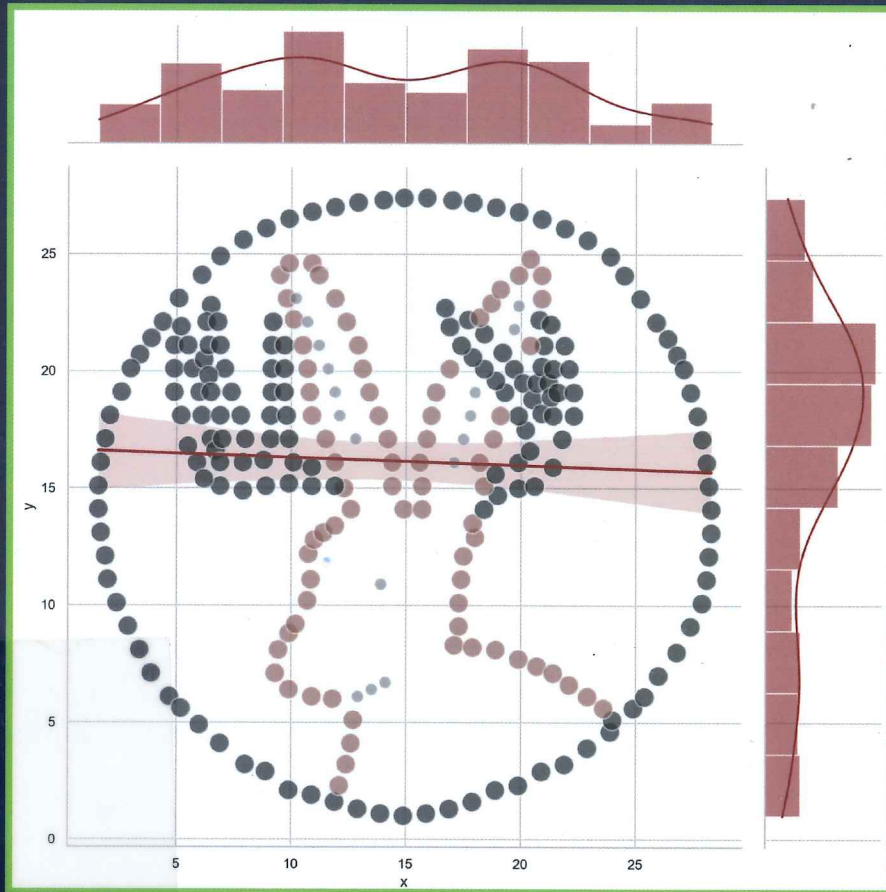


THE PYTHON SERIES

STATISTICS AND DATA VISUALISATION WITH PYTHON



JESÚS ROGEL-SALAZAR



CRC Press
Taylor & Francis Group

A CHAPMAN & HALL BOOK

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Statistics and Data Visualisation with Python



Jesús Rogel-Salazar



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