New Era Electronics: a Lecture Notes Series • Volume 2

Quantum Communication

The Physical Layer of Future Optical Networks

Mahdi Hosseini

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Purdue University, USA

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