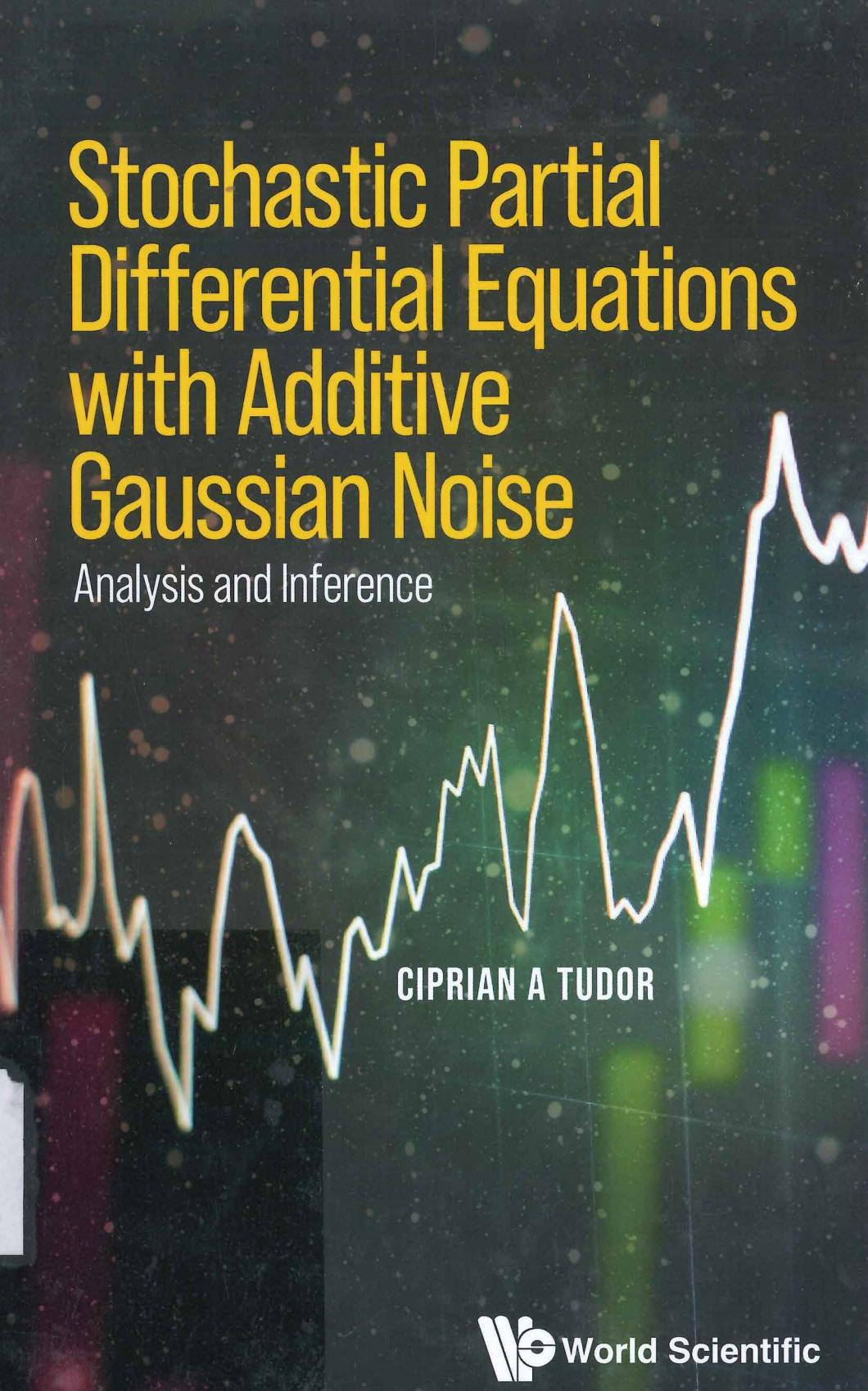


Stochastic Partial Differential Equations with Additive Gaussian Noise

Analysis and Inference

The background of the book cover features a dark, textured surface with a subtle grid pattern. Overlaid on this are several thin, wavy lines in various colors (yellow, orange, red, green, blue) that resemble light trails or stochastic processes. Small, glowing particles of different sizes and colors (yellow, orange, green, blue) are scattered across the surface, creating a sense of depth and motion.

CIPRIAN A TUDOR



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Stochastic Partial Differential Equations with Additive Gaussian Noise

Analysis and Inference

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