



Fundamentals of Power Systems Analysis 1

Problems and Solutions

Mostafa Eidiani
and **Vahideh Heidari**



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